

# **Money, Finance and Growth**

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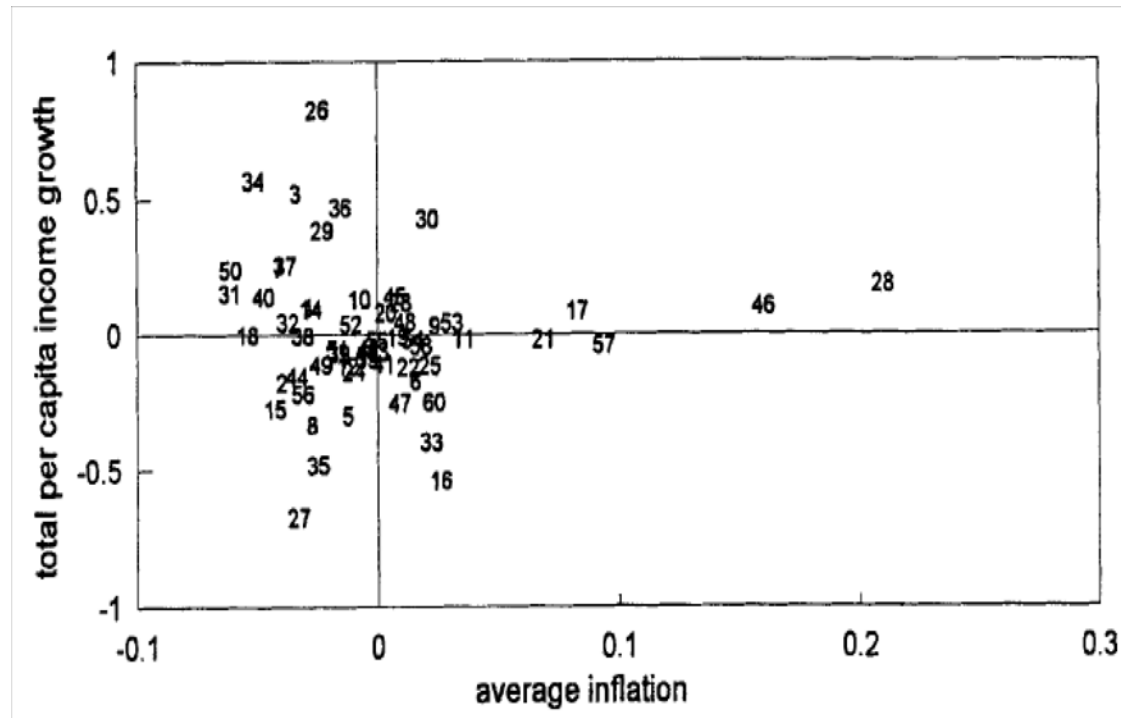
# **I. Introduction**

## **A. Empirical Regularities**

### **1. Money and growth (Friedman-Schwartz; Walsh, ch. 1):**

- a. positive correlation in levels**
- b. largely negative correlation in growth rates**
- c. presence of a liquidity effect**

**Summer-Heston data (1960-85, excluding poor quality data, 60 countries):**



- Note:**
- (i) **High inflation countries:** 28 = Indonesia, 46 = Iceland, 57 = Turkey, 17 = Mexico, 21 = Columbia;
  - (ii) **High growth countries:** 26 = Hong Kong, 34 = Singapore, 3 = Morocco, 30 = South Korea, 29 = Japan.

- 2. Finance and growth (Becsi-Wang 1997; Levine 1997):**
  - a. positive correlation in levels (Goldsmith 1969, McKinnon 1973)**
  - b. mixed relation in growth rates:**
    - i. zero correlation for OECD (Fernandez-Galetovic 1994)**
    - ii. weakly negative correlation for Latin America (DeGregorio-Guidotti 1995)**
    - iii. strongly positive correlation for Asia (King-Levine 1993)**

| <b>Financial Deepening</b> | <b>Per Capita Income</b>              |   |   |
|----------------------------|---------------------------------------|---|---|
|                            | <b>High</b>                           | <b>Middle</b>                             | <b>Low</b>  |
| <b>High</b>                | <b>US, France, Italy, Switzerland</b> | <b>Chile, Venezuela</b>                   | <b>Kenya, Jamaica<br/>Honduras</b>                    |
| <b>Middle</b>              | <b>Norway, Germany, Denmark</b>       | <b>Malaysia<br/>Trinidad &amp; Tobago</b> | <b>Liberia, Uganda</b>                                |
| <b>Low</b>                 |                                       | <b>Ireland, Hungary, Yugoslavia</b>       | <b>Sri Lanka, Philippines<br/>Zimbabwe, Indonesia</b> |

- Notes:**
- (i) Per capita income is measured by 1985 real GNP per capita in US\$ at 1980 constant prices where high income takes values of \$7,500 or above, middle income from \$3,000 to \$6,000, and low income up to \$2,000.**
  - (ii) Financial deepening is measured by the financial intermediation ratio (FIR) defined as in Goldsmith (the ratio of M to GNP) where high deepening takes values of 13% or above, middle deepening from 8% to 12%, and low deepening up to 7%.**
  - (iii) Gaps are allowed to ensure more definitive classification.**

### **3. Key Literature**

- **Use of money:**
  - **money in the utility function (direct value, wealth or transactions time reduction): Samuelson (1947), Patinkin (1965), Sidrauski (1967), Brock (1974), Wang-Yip (1992a), Wang-Yip (1992b)**
  - **cash in advance: Tsiang (1966), Clower (1967), Lucas (1980), Stockman (1981), Lucas-Stokey (1987), Cooley-Hansen (1989), Wang-Yip (1992a), Gomme (1993), Ireland (1994), Jones-Manuelli (1995)**
  - **transactions cost: Saving (1973), Drazen (1979), Grossman-Weiss (1983), Rottemberg (1984), Wang-Yip (1992a), Jha-Wang-Yip (2002)**
  - **medium of intergenerational transactions: Samuelson (1958), Wallace (1980), McCullum (1983), Wang (1993), Van der Ploeg-Alogoskoufis (1994)**
  - **liquidity service: Feenstra (1986), Chang-Chang-Lai-Wang (2008)**

- **money and search: Wicksell (1898), Jones (1976), Wang (1987), Kiyotaki-Wright (1989, 1993), Trejos-Wrighth (1995), Lagos-Wright (2002), Laing-Li-Wang (2007, 2013)**
  
- **Major Roles of Financial Intermediation:**
  - **liquidity management: Diamond-Dybvig (1993), Bencinvinga-Smith (1991)**
  - **risk pooling: Townsend (1978), Greenwood-Jovanovic (1990), Bencivenga-Smith (1993)**
  - **effective monitoring: Williamson (1986), Greenwood-Jovanovic (1990)**
  - **funds pooling: Besley (1994), Becsi-Wang-Wynne (1999)**

## **II. Money in Dynamic General Equilibrium: Wang-Yip (1992)**

- **Provide a unified framework to study 3 main dynamic general equilibrium models of money**
- **Main issue: is money superneutral?**
- **Tobin (1965): via asset substitution, higher money growth reduces real balances but encourages capital accumulation and output growth (Tobin effect)**
- **Sidrauski (1967): even if money is valued directly, money growth has no effect on steady-state output**
- **Stockman (1981): higher money growth reduces real balances, limits capital investment, and lowers output growth (reversed Tobin effect)**



**a. Money in the Utility Function**

$$\max \int_0^{\infty} W(c(t), \ell(t), m(t)) e^{-\rho t} dt$$

$$\text{s.t. } c(t) + \dot{k}(t) + \dot{m}(t) = f(k(t), \ell(t)) - nk(t) - (\pi(t) + n)m(t) + \tau(t)$$

● **FOCs and S-S BC:**

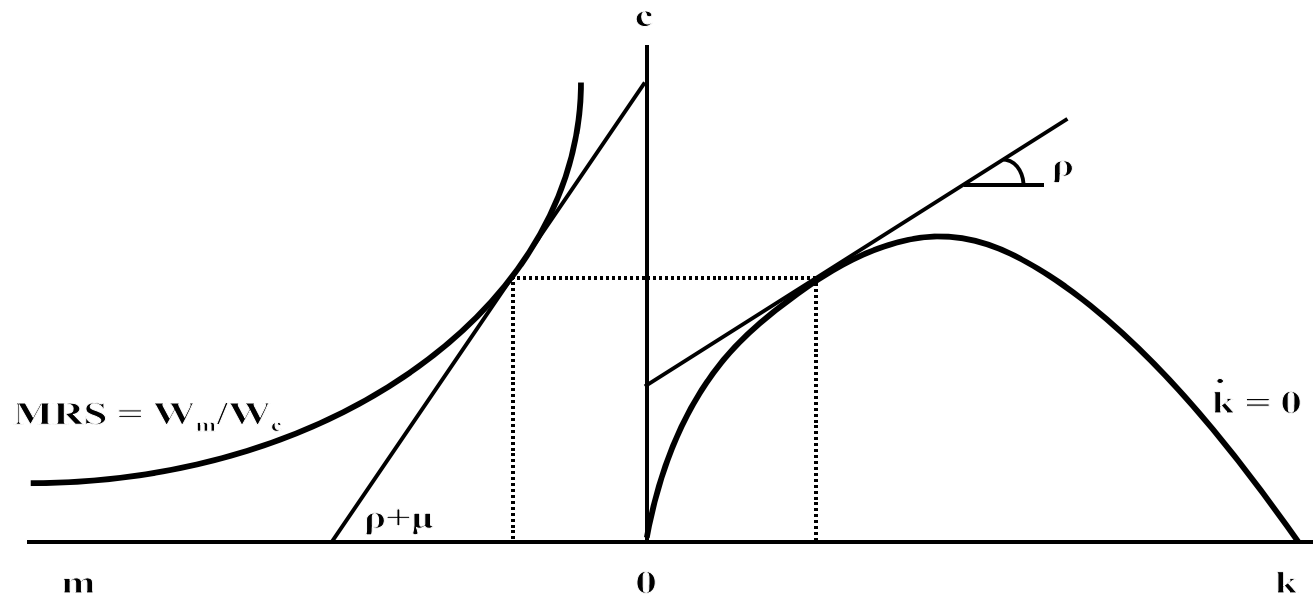
$$f_k(k, \ell) = \rho + n$$

$$W_c(c, \ell, m) f_\ell(k, \ell) = -W_\ell(c, \ell, m)$$

$$W_m(c, \ell, m) = (\rho + \mu) W_c(c, \ell, m) .$$

$$c = f(k, \ell) - nk.$$

- **Equilibrium**



- **Comparative statics**

higher  $\mu \Rightarrow W_m/W_c$  increases

$\Rightarrow m$  lowers (if  $W_{cl} < 0$ , i.e.,  $c$  and  $x$  are complem.)

$\Rightarrow$  (W1)  $W_{cm} > 0$ ,  $W_{\ell m} > 0$ :  $c$ ,  $\ell$ ,  $k$  all fall

(W2)  $W_{cm} < 0$ ,  $W_{\ell m} < 0$ :  $c$ ,  $\ell$ ,  $k$  all rise

**b. Cash in Advance**

$$\max \int_0^{\infty} U(c(t), 1 - \ell(t)) e^{-\rho t} dt$$

$$\text{s.t. } c(t) + \dot{k}(t) + \dot{m}(t) = f(k(t), \ell(t)) - nk(t) - (\pi(t) + n)m(t) + \tau(t)$$

$$m(t) \geq c(t) + \Gamma \dot{k}(t)$$

where  $\Gamma = 0, U_\ell = 0 \Rightarrow$  Lucas;  $\Gamma = 1, U_\ell = 0 \Rightarrow$  Stockman

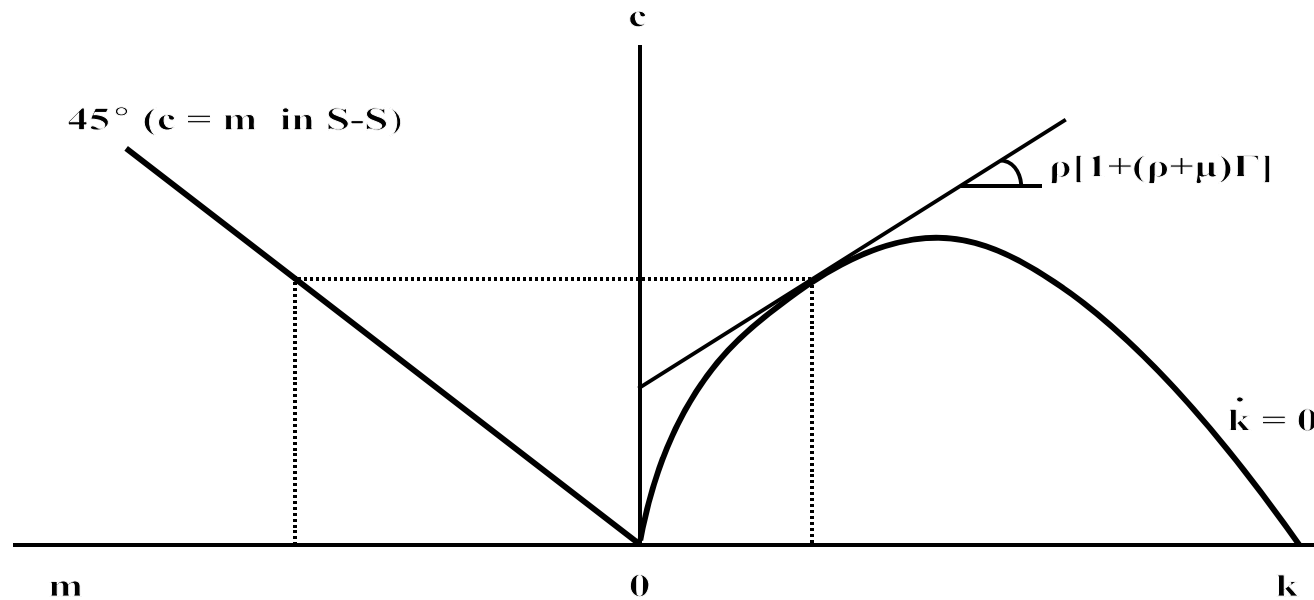
● **FOCs:**

$$f_k = \rho + n + \rho(\rho + \mu)\Gamma$$

$$f_\ell U_c = (1 + \rho + \mu)U_x .$$

**Thus, money growth affects MPK directly**

- **Equilibrium**



- **Comparative statics**

- higher  $\mu \Rightarrow k$  decreases
- $\Rightarrow \ell$  lowers ( $f_{k\ell} > 0$ )
- $\Rightarrow y$  and  $c$  fall
- $\Rightarrow (1-\ell)$  reduces ( $U_{cx} > 0$ ) and so  $\ell$  rises
- $\Rightarrow$  net effect on  $\ell$  ambiguous

### c. Transactions Cost Model

$$\max \int_0^{\infty} U(c(t), 1 - \ell(t) - T(t))e^{-\rho t} dt$$

$$\text{s.t. } \overline{c(t) + \dot{k}(t) + \dot{m}(t) = f(k(t), \ell(t)) - nk(t) - (\pi(t) + n)m(t) + \tau(t)}$$

where  $\overline{T(t) = T(c(t), m(t))}$ , satisfying:

$$\mathbf{T}_c > \mathbf{0}, \mathbf{T}_m < \mathbf{0}, \mathbf{T}_{cc} < \mathbf{0}, \mathbf{T}_{mm} > \mathbf{0}, \mathbf{T}_{mc} \leq \mathbf{0}$$

- **FOCs:**

$$f_k = \rho + n$$

$$f_\ell U_c = (1 + T_c f_\ell) U_x$$

$$-T_m f_\ell = \rho + \mu ,$$

where money growth affects output via **MPL**

- **Comparative statics**

**higher  $\mu \Rightarrow k/\ell$  unchanged, as does  $f_\ell$**   
 **$\Rightarrow (-T_m)$  increases and hence  $m$  decreases**  
 **$\Rightarrow T$  increases and  $\ell$  decreases**  
 **$\Rightarrow k$  decreases, as does  $c$**   
 **$\Rightarrow$  but the decrease in  $c$  lowers  $T$**   
 **$\Rightarrow$  net effect on  $x = 1 - \ell - T$  ambiguous**

**d. Qualitative equivalence between the three models if  $W_{cl} < 0$ ,  $W_{cm} > 0$ ,  $W_{\ell m} > 0$ ,  $\Gamma = 0$ ,  $T(c,m) = 0$  if  $c \leq m$  and  $= 1$  otherwise**

**e. Questions: As the three most used "conventional" approaches to money seem to yield qualitatively similar theoretical findings, can "newer" approaches deliver more insights along the lines of money, inflation and growth?**

### III. Money and Endogenous Growth: Jones and Manuelli (1995)

- Modified Cooley-Hansen (1989) model to permit endogenous growth

#### a. Basic One-Sector Endogenous Growth Model of Money

- Consumer's optimization:

$$\begin{aligned} & \max \sum_t \beta^t u(c_{1t}, c_{2t}, 1 - n_t) \\ \text{s.t.} \quad & m_t + b_{t+1} \leq v_t, \\ & p_{1t}c_{1t} \leq m_t, \\ & v_{t+1} \leq (v_t - m_t - b_{t+1}) + (m_t - p_{1t}c_{1t}) - p_{2t}c_{2t} - p_{1t}x_t \\ & \quad + p_{1t}w_t n_t + p_{1t}r_t k_t + (1 + R_{t+1})b_{t+1} + T_t, \\ & k_{t+1} \leq (1 - \delta)k_t + x_t, \end{aligned}$$

where  $v$  = nominal wealth,  $T$  = money transfer ( $M_{t+1} - M_t$ ),  
 $R$  = nominal interest rate,  $w, r$  = real factor prices  
 $p_i$  = nominal price of  $i$  (1 & 2 are cash & credit good)  
 $p_i = p$  if both goods are produced

- **Firm's optimization**

$$\max \pi_t = p_{1t}c_{1t} + p_{2t}c_{2t} + p_{1t}x_t - p_{2t}r_t k_t - p_{1t}w_t n_t$$

$$\text{s.t. } c_{1t} + c_{2t} + x_t \leq F(k_t, n_t)$$

- **FOCs**

$$\frac{u_1(t) F_2(t)}{u_3(t)} = 1 + R_{t+1},$$

$$\frac{u_1(t)}{u_1(t+1)} = \frac{(1 + R_{t+1})}{(1 + R_{t+2})} \beta [1 - \delta + F_1(t+1)]$$

$$\frac{u_1(t)}{u_2(t)} = 1 + R_{t+1},$$

$$1 + R_{t+2} = \frac{p_{t+1}}{p_t} [1 - \delta + F_1(t+1)],$$

and the CIA holds for equality in equilibrium



- **Asymptotic BGP equilibrium**

(A1)  $F = Ak + Dk^\alpha n^{1-\alpha}$ , with  $\beta(1 - \delta + A) > 1$

(A2)  $u = [(c_1^{-\lambda} + \eta c_2^{-\lambda})^{-1/\lambda} (1 - n)^\psi]^{1-\sigma} / (1 - \sigma)$ , with  $\sigma > 1, \lambda \geq -1$

$$\begin{aligned} \gamma^\sigma &= \beta [1 - \delta + A] \\ \pi\gamma &= \mu \\ 1 + R &= \pi [1 - \delta + A] \\ c_2/c_1 &= [\eta(1 + R)]^{1/(1 + \lambda)} \end{aligned}$$

where  $\mu = M_{t+1}/M_t$ ,  $\pi = p_{t+1}/p_t$

Thus,  $r = A - \delta$  and  $\gamma = [\beta(1 + r)]^{1/\sigma} = \mu/\pi$  (growth rate of  $m/p$ )

- **Comparative statics**

- money is superneutral in the narrow sense ( $\gamma$  independent of  $\mu$ )
- higher  $\mu$  leads to higher  $\pi$ , higher  $R$ , and higher  $c_2/c_1$  (the only source of nonsuperneutrality in the broad sense)

## b. Two-Sector Endogenous Growth Model of Money

- Consumer's optimization:

$$\max \sum_t \beta^t u(c_{1t}, c_{2t}, 1 - n_t)$$

$$\text{s.t. } m_t + b_{t+1} \leq v_t,$$

$$c_{1t} p_t \leq m_t,$$

$$\begin{aligned} v_{t+1} \leq & (v_t - m_t - b_{t+1}) + (m_t - p_t c_{1t}) - p_t c_{2t} \\ & - p_t x_{kt} - p_t x_{ht} + p_t w_t n_t h_t + p_t r_t k_t \\ & + (1 + R_{t+1}) b_{t+1} + T_t, \end{aligned}$$

$$k_{t+1} \leq (1 - \delta_k) k_t + x_{kt},$$

$$h_{t+1} \leq (1 - \delta_h) h_t + x_{ht},$$

where physical/human capital investments are credit goods and the final good production function is given by,  $F(k, nh) = Ak^\alpha(nh)^{(1-\alpha)}$ , implying  $k/h = \alpha/(1-\alpha)$  if  $\delta_k = \delta_h$

- Firm's optimization stays the same (except modified production)
- Asymptotic BGP equilibrium with  $\delta_k = \delta_h$

2 x 2 system in  $(\gamma, n)$ :

(modified GR)  $\gamma^\sigma = \beta [1 - \delta + \alpha A n^{1-\alpha} [(1-\alpha)/\alpha]^{1-\alpha}]$

(labor tradeoff)  $\gamma = 1 - \delta + B n^{1-\alpha} \left( 1 - \frac{(1-\alpha)(1-n)}{\psi n f(\mu, \gamma)} \right)$

where  $f(\mu, \gamma) = 1 + \frac{\mu \beta^{-1} \gamma^{(\sigma-1)} - 1}{1 + \eta^{1/(1+\lambda)} (\mu \beta^{-1} \gamma^{(\sigma-1)})^{1/(1+\lambda)}}$

- Comparative statics
- money is generally nonsuperneutral even in the narrow sense
- for  $\lambda > 0$  ( $c_1, c_2$  complements): higher  $\mu$  reduces  $c_1$  and  $c_2$ , lowering  $n$  and  $\gamma$
- for  $\lambda < 0$  ( $c_1, c_2$  substitutes): higher  $\mu$  reduces  $c_1$  but raises  $c_2$ , lowering  $n$  and  $\gamma$  if  $\eta$  is sufficiently small (CIA binds for almost all purchases)

#### IV. Finance and Growth - A First Look: Benci and Wang (1997)

(i) **Key:** Add a banking sector to the AK-model of endogenous growth

(ii) **A Benchmark AK-model without the Financial Sector:**

a. **optimization:**

$$\max U = \int_0^{\infty} \frac{c^{1-\alpha} - 1}{1-\alpha} e^{-\rho t} dt$$

$$s.t. \dot{k} = Ak - \eta k - c, \quad k(0) = k_0 > 0.$$

b. **Key relationships without a banking sector:**

● **Keynes-Ramsey equation:**  $\theta = \frac{\dot{c}}{c} = \frac{r - \rho}{\alpha} \Rightarrow r = \rho + \alpha\theta$  (UU)

● **Production efficiency:**  $\delta = A - \eta$  (YY)

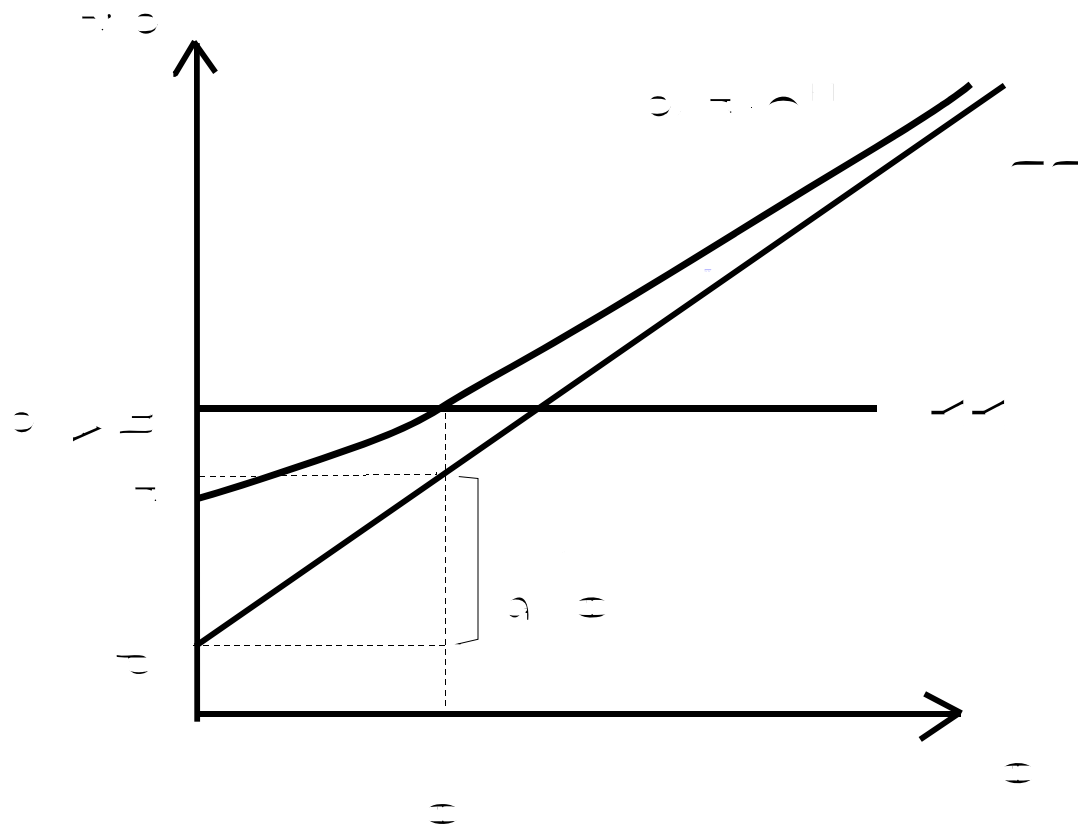
● **In the absence of an active banking sector:**  $r = \delta$

### **(iii) Incorporation of the Financial Sector into the AK-Model**

- **A key ingredient is to recognize the loan-deposit interest differential. With active banking, deposits are transformed into loans, but such operations are not costless.**
- **In the absence of reserve requirement, loanable funds equilibrium implies that deposits equal to loans, denoted by  $x$  (in real values)**
- **Denote the unit financial intermediation cost as  $C_{FI}$ , which is decreasing as an economy develops (i.e.,  $\partial C_{FI}/\partial \theta < 0$ ; see Lehr and Wang 1999 for empirical documentation).**
- **By competitive banking (perfectly competitive or monopolistically competitive), banks must reach zero profit:  $\text{profit} = \delta x - rx - C_{FI} x = 0$ , or,  $\delta = r + C_{FI}(\theta)$ .**
- **The financial markup can be derived as:  $\mu = \delta - r = C_{FI}(\theta)$ , which depends negatively on the stage of economic development measured by the rate of growth  $\theta$ .**

## (v) BGP Equilibrium

- Along a BGP, the endogenous growth rate must be pinned down by the loan rate and the production technology, whereas the preferences determines the deposit rate.
- The BGP equilibrium  $(\theta, \delta)$  is determined when the YY locus intersects with the markup locus, which can then be used, in conjunction with UU, to pin down equilibrium  $r$ .



- **Comparative statics:**

- **production innovation:**  $A \nearrow \Rightarrow \delta \nearrow, r \nearrow, \mu \searrow, \theta \nearrow$
- **banking innovation:** exog.  $C_{FI} \searrow \Rightarrow \delta$  unchanged,  $r \nearrow, \mu \searrow, \theta \nearrow$
- **annuity innovation:**  $\rho \searrow \Rightarrow \delta, \theta \nearrow, r \nearrow, \mu \nearrow$
- **effective monitoring:**  $A \nearrow$  and  $C_{FI} \searrow \Rightarrow \delta \nearrow, r \nearrow, \mu \searrow, \theta \nearrow$
- **technological and annuity innovation:**  $A \nearrow$  and  $\rho \searrow \Rightarrow \delta \nearrow, r ? (\searrow$  if direct effect dominates),  $\mu \nearrow, \theta \nearrow$
- **limited bank entry:** more local market power  $\Rightarrow \mu \nearrow, \theta ?$  (Smith vs. Schumpeter)

## V. Liquidity Management, Financial Intermediation and Growth: Bencivenga-Smith (1991)

- **The role of financial intermediation: liquidity management.**
- **Liquid investment is not as productive as illiquid investment. To accommodate illiquid investment and possible withdrawals, banks hold liquid reserves. However, should there be unexpected withdrawals, banks may face a illiquidity problem.**

- The model generalizes Diamond-Dybvig (1983) by incorporating liquidity management into an endogenous growth framework.

a. The Model

- 3-period overlapping-generations (pop = 1), supplying 1 unit of labor only when young and consuming when middle-aged and old
- Production:  $y = \bar{k}^{-1-\theta} k^\theta L^{1-\theta}$  (Romer)
- Labor demand per entrepreneur:  $MPL = w$
- Utility:  $U = -(c_2 + \varphi c_3)^{-\gamma} / \gamma$ ,  $\gamma > -1$  since  $\sigma = 1/(1+\gamma)$   
 where  $\varphi = 0$  with probability  $1-\pi$  (early withdrawers)  
 $\varphi = 1$  with probability  $\pi$  (entrepreneurs)
- Investment returns:
  - liquid investment: return =  $n > 0$  (safe return)
  - illiquid investment:
    - return after 1 period =  $x \in [0, n)$  (liquidated scrap value  $< n$ )
    - return after 2 period =  $R > n$  (LT investment return  $> n$ )



- **Labor market equilibrium:**  $\pi L = 1$  (young's labor supply)
- **Factor prices:**
  - $w = (1-\theta)k\pi^\theta$
  - $r_k = \theta\pi^{\theta-1}$
- **With financial intermediation, all wages are deposited in banks.**
- **Banks:**
  - have asset management portfolio of  $\{z, q\}$ , choosing a fraction  $z$  in liquid investment and  $q$  in illiquid investment, where  $z + q = 1$
  - have liabilities, paying
    - $r_1$  to 1-period deposits
    - $r_2$  to 2-period deposits without withdrawals (capital)
    - $r_0$  to liquidated 2-period deposits (scraped for consumption).
- **Banks' resources constraints (payments = revenues):**
  - 1-period:  $(1-\pi)r_1 = \alpha_1 n z + \alpha_2 x q \quad (\alpha_1 + \alpha_2 = 1)$
  - 2-period:  $\pi r_2 = (1-\alpha_2) R q$
  - 2-period scraped:  $\pi r_0 = (1-\alpha_1) n z$

- **Gurley-Shaw's bank (in the interest of the depositors, i.e., banks as coalitions formed by the young): choose  $\{q, z, \alpha_1, \alpha_2, r_1, r_2, r_0\}$  to:**

$$\max \quad EV = (1 - \pi) \left[ -\frac{(r_1 w)^{-\gamma}}{\gamma} \right] + \pi \left[ -\frac{(\theta \pi^{\theta-1} r_2 w + r_0 w)^{-\gamma}}{\gamma} \right]$$

**s.t.  $\alpha_1 + \alpha_2 = 1, z + q = 1$  and 3 bank resources constraints**

## b. Results

- **Equilibrium decisions: with  $r_k R = \theta \pi^{\theta-1} R > n$ ,**
  - $\alpha_1 = 1$  (2-period reserve always in capital)
  - $\alpha_2 = 0$  (no pre-mature liquidation of capital)
  - $r_0 = 0$  (paying nothing to liquidated consumption)
- **Financial intermediation emerges with *rate-of-return dominance***
  - it requires large  $\gamma$  (or small intertemporal substitution)
  - intuitively, small intertemporal substitution is equivalent to more risk aversion intertemporally, thus giving a stronger role for banks to form.

- **Key finding: the rate of growth with financial intermediation is higher than without it if  $x$  is sufficiently small.**

**Remark:** Although the current model assumes forced savings (no value of period-1 consumption), main results are robust to such an extension.

## **VI. Finance, Investment, and Growth: Aghion-Bolton (1997)**

- **The Aghion-Bolton model can be regarded as an extension of Banerjee-Newman (1993) by allowing full dynamics of wealth evolution with:**
  - (i) endogenous occupational choice**
  - (ii) credit market imperfections**
  - (iii) nonstationary distribution (cf. Hopenhayne-Prescott)**

## a. The Model

- 1-period lived agents of with unit mass with bequest motive, one unit of time endowment, and heterogeneous initial wealth  $w \sim G_t(w)$

### Occupational choice:

- Home production: return  $n > 0$  (small)
- Entrepreneurial activity:

$$F(k,1) = \begin{cases} r & \text{for } k \geq 1 \text{ (fixed cost), with prob.} = p \\ 0 & \text{for } k \geq 1, \text{ with prob.} = 1 - p \\ 0 & \text{for } k < 1 \end{cases}$$

where  $p = \text{effort with effort cost } C(p) = \frac{rp^2}{2a}, a \in (0, 1]$

- Mutual fund deposit: safe return  $A_t w_t$  (no labor input)
- Preferences: Leontief in consumption and bequest  
 $U = [\delta(1 - \delta)]^{-1} \min\{(1 - \delta)c, \delta b\} - C(p)$
- Budget Constraint:  $c + b = w$

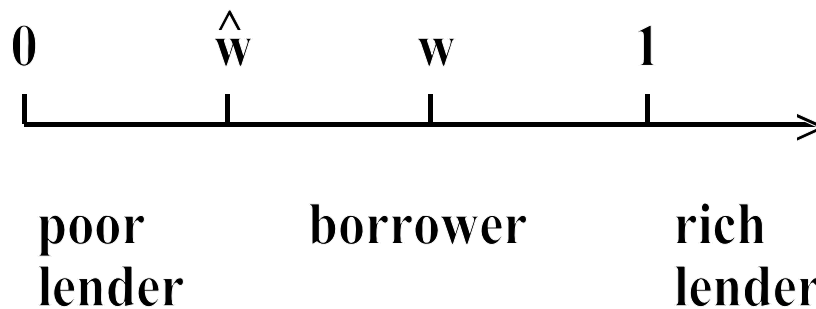


- **Occupational choice and investment decision:**

- **Potential borrower ( $w < 1$ ):**  $\max_p \quad pr - p(1-w)\rho(w) - C(p),$

implying  $p(w) = a[1 - (\frac{1-w}{r})\rho(w)]$

- **Rich lender ( $w \geq 1$ ):**  $\max_p \quad pr - C(p),$       implying  $p(w) = a$



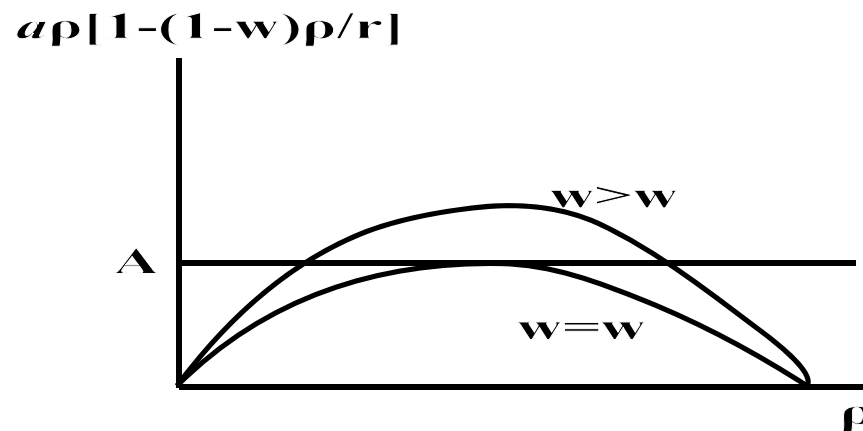
$$\text{loan} = 1 - w$$

### c. Atemporal Equilibrium

- Rate of return equalization to lenders:

$$p(w)\rho = A \quad \Rightarrow \quad \rho(w) = \frac{r}{2(1-w)} \left[ 1 - \sqrt{1 - \frac{4(1-w)A}{ar}} \right] \quad \forall w \in [\underline{w}, 1]$$

where  $\underline{w} = 1 - ar/(4A)$  with  $\rho' > 0$  ( $p' > 0$ )



$w \in [0, \underline{w}) \Rightarrow$  no loan supply  $\Rightarrow$  unable to borrow

- **Rate of return equalization to borrowers**

$$p(w_C)r - p(w_C)\rho(w_C)(1-w_C) - C(p(w_C)) - 1 = Aw_C + n$$

=> willing to borrow if  $w > w_C$  or  $A < (3/8)ar - n - 1$

- **Condition CR:**  $\exists \underline{w} > 0$  and  $w > w_C$ , or,  $ar/4 < A < (3/8)ar - n - 1$
- **Under condition CR, we have:**  $\forall w \in (w_C, \underline{w})$ , they are willing to borrow but unable to obtain loan => **equilibrium credit rationing**

#### d. Full Equilibrium

- **Wealth evolution:**  $w_{t+1} = \begin{cases} (1-\delta)(Aw_t + n) & \text{for } w_t \in [0, \hat{w}_t] \\ g_t(w_t, \theta_t) & \text{for } w_t \in [\hat{w}_t, \infty) \end{cases}$

where  $\hat{w}_t = \max\{\underline{w}, w_C\}$ ,  $\theta_t =$  indicator function for success, and

$$g(w,1) = \begin{cases} (1-\delta)[r - (1-w)\rho(w)] & w < 1 \\ (1-\delta)[r + (w-1)A] & w \geq 1 \end{cases} \quad g(w,0) = \begin{cases} 0 & w < 1 \\ (1-\delta)(w-1)A & w \geq 1 \end{cases}$$

$$prob.(\theta = 1|w) = h(w) = \begin{cases} p(w) & w < 1 \\ a & w \geq 1 \end{cases}$$



- **Distribution converges in weak\* topology in Polish space**
- **Additional assumptions:**
  - (A3) (incentive to lend)  $\frac{ar}{4}(1-\delta) > 1$
  - (A4) (rapid accumulation)  $\frac{3}{8}ar(1-\delta) > 1+n$
- **Safe rate of return:**
  - $A_t \leq \frac{1}{1-\delta} \quad \forall t \geq T$  (ow, unbounded wealth=>excess fund supply)
  - under (A3), CR does not exist for  $A_t \in [1, 1/(1-\delta)]$
  - under (A3) and (A4),  $A_t \rightarrow 1$  in finite time
- **Trickle-down:**
  - CR exists in early stage of development when  $A_t$  is high
  - As  $w_t \uparrow$  over time,  $A_t$  falls in  $[1, 1/(1-\delta)] \rightarrow 1 \Rightarrow$  no CR
  - Intuition: the rich trickle down increasing supply of loan and enabling the poor to borrow and invest by lowing capital cost  $A_t$

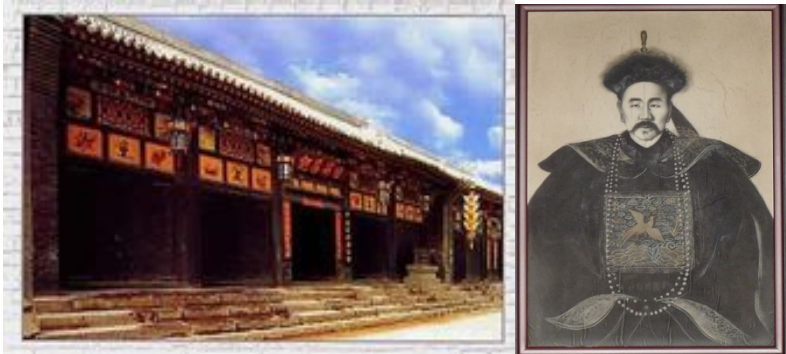
## VII. Big Push or Big Crash:

### A Retrospect of Financial Crises

- Merchant of Venice (Shakespeare 1596-98):
  - Antonio: merchant of Venice, intermediary/loan guarantor
  - Bassanio: loan demander, suitor to Portia - a beautiful rich heiress of Belmont
  - Shylock: rich Jew, moneylender (loan supplier)
  - Usury/Usance (interest/duration of loan): one pound of Antonio's flesh by a bond date
  - Productivity of loan: gaining Portia's love, which is high risk but potentially high return
  - When Antonio's ships were reported lost at sea, Antonio was at risk of losing a pound of flesh (individual crisis)



## a. Historical Financial Crises



- Crises of Chinese Money Stores/Piao-Hau:
  - Hui-gang's (徽幫) Fu-Kang Money Store (阜康錢莊) by Shieh-Yen Hu (胡雪巖) and Gin-gang's (晉幫) Shan-Hsi Piao-Hau (山西票號) by Lui-Tai Lei (雷履泰; after the turn of 20<sup>th</sup> century, Shiang-Hsi Kung became the leader of this group) were the two largest financial institutions in the turn into the 20<sup>th</sup> century
  - Bankruptcy of Fu-Kang Money Store suddenly occurred as a result of losing government support
  - Financial contagion caused early withdrawal and illiquidity of Shan-Hsi Piao-Hau
  - **Lesson: financial crisis can come suddenly, being large scale and wide spread with even high performers failing**
  - A view of Gin-gang's Money Store (日昇昌票號, 山西平遙, 1823): <http://www.youtube.com/watch?v=fUrD4Gg59ls>

## b. Major Financial Crises Since 1900

- Argentina (1985, 1989, 1992, 1999-2001), Bolivia (1985), Brazil (1989), Chile (1982), Mexico (1982, 1987, 1994)
- Israel (1985), Russia (1998)
- U.S. (1907, 1929, 1984-85), Spain (1977), Norway (1987), Finland (1991), Sweden (1991), Japan (1992),
- A group of Asian countries (1997): Hong Kong, Indonesia, Korea, Malaysia, Philippines, Thailand
- Worldwide Financial Tsunami (2008-09) caused by subprime mortgage crisis in the U.S.

## c. A First Look at Financial Crises

- Duration (in years) and depth (in % of cumulative GNP losses) of financial crises over the past century:

| Crises          | 1880-1913        | 1919-1939        | 1945-1971       | 1973-1997        |
|-----------------|------------------|------------------|-----------------|------------------|
| Currency Crises | 2.6 yrs<br>8.3%  | 1.9 yrs<br>14.2% | 1.8 yrs<br>5.2% | 2.1 yrs<br>5.9%  |
| Banking Crises  | 2.3 yrs<br>8.4%  | 2.4 yrs<br>10.5% | 0 yrs<br>0%     | 2.6 yrs<br>6.2%  |
| Twin Crises     | 2.2 yrs<br>14.5% | 2.7 yrs<br>15.8% | 1.0 yrs<br>1.7% | 3.8 yrs<br>18.6% |

## d. The 1997 Asian Financial Crises

- This episode has puzzled many economists:
  - trade deficit as a poor predictor: Sacks-Tornell-Velasco (1996)
  - no high inflation associated with fiscal or exchange rate collapse crises except Indonesia (Chang-Velasco 1998, Burnstein-Eichenbaum-Rebelo 1998)
  - no excessive foreign debt except Indonesia and Philippines ( $> 1/2$  of GDP)
  - no severe illiquidity problem

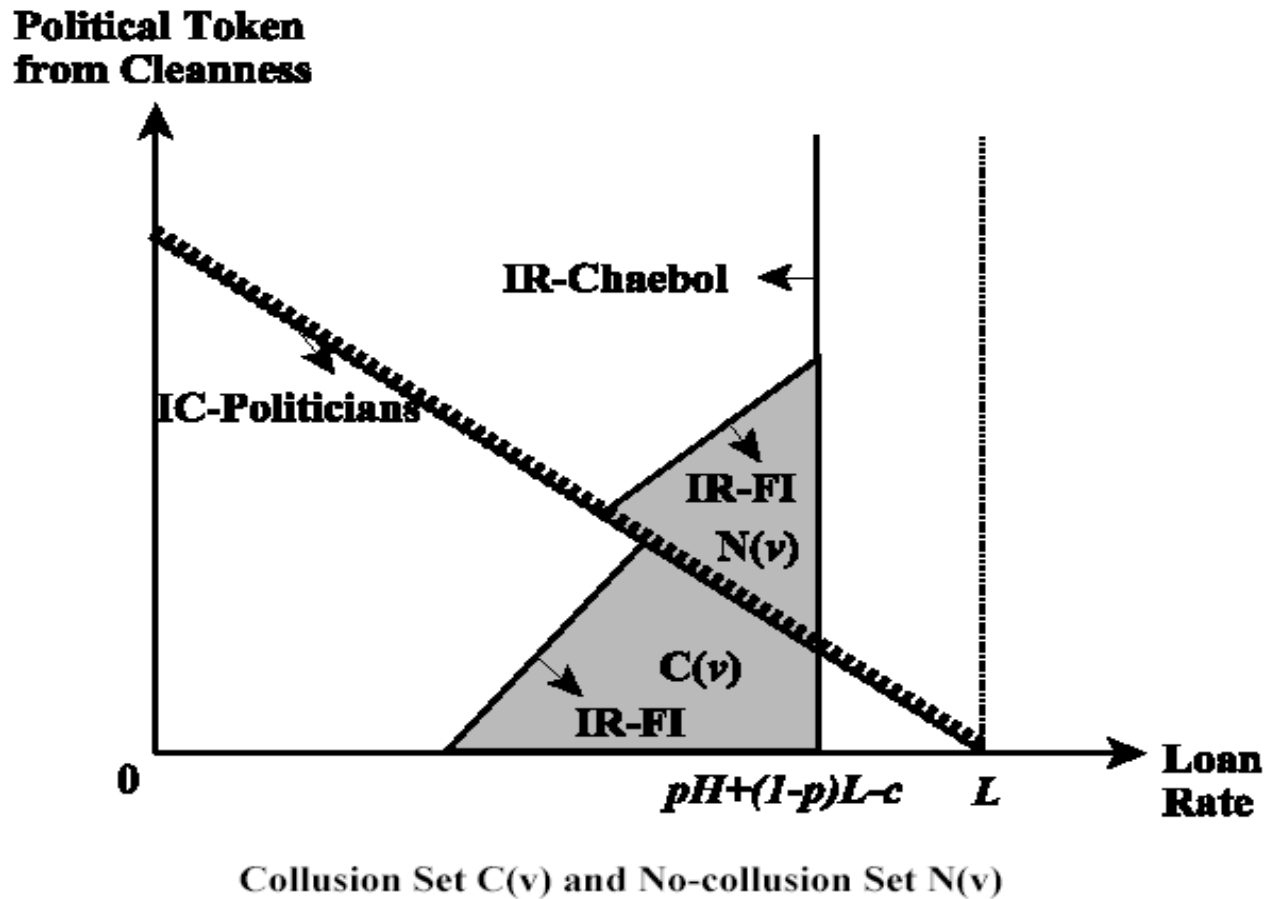
|                          | CHI   | TWN   | SNG   | HKG   | THD   | MAL   | KOA   | IND   | PHN   |
|--------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| <b>GDP Growth (%)</b>    |       |       |       |       |       |       |       |       |       |
| 1990                     | 9.19  | 7.60  | 7.27  | 4.97  | 8.41  | 8.42  | 9.13  | 6.95  | -0.51 |
| 1995                     | 10.55 | 6.00  | 8.75  | 4.40  | 8.68  | 9.46  | 8.94  | 8.22  | 4.76  |
| 1996                     | 9.34  | 5.70  | 7.32  | 5.00  | 6.66  | 8.20  | 7.13  | 7.98  | 5.67  |
| <b>Inflation</b>         |       |       |       |       |       |       |       |       |       |
| 1990                     | 6.40  | 3.60  | 3.40  | 11.60 | 5.70  | 4.40  | 9.30  | 9.40  | 18.70 |
| 1995                     | 5.50  | 3.70  | 1.79  | 8.59  | 5.69  | 5.28  | 4.49  | 9.43  | 8.11  |
| 1996                     | 6.20  | 3.10  | 1.32  | 5.98  | 5.85  | 3.56  | 4.96  | 8.03  | 8.41  |
| <b>Savings/GDP</b>       |       |       |       |       |       |       |       |       |       |
| 1990                     | 37.8  | 29.3  | 45.3  | 35.6  | 32.2  | 29.1  | 35.7  | 31.8  | 17.9  |
| 1995                     | 40.1  | 28.0  | 51.1  | 31.6  | 37.6  | 29.8  | 35.1  | 27.7  | 17.2  |
| 1996                     | 42.1  | 28.0  | 51.3  | 32.0  | 33.6  | 37.0  | 33.3  | 28.7  | 18.3  |
| <b>Trade Surplus/GDP</b> |       |       |       |       |       |       |       |       |       |
| 1990                     | 3.02  | 6.70  | 9.45  | 8.40  | -8.74 | -2.27 | -1.24 | -4.40 | -6.30 |
| 1995                     | 1.02  | 1.90  | 17.93 | -2.21 | -9.00 | -13.5 | -1.91 | -4.25 | -5.06 |
| 1996                     | -0.34 | 5.20  | 16.26 | 0.58  | -9.18 | -5.99 | -4.89 | -3.41 | -5.86 |
| <b>Gov't Surplus/GDP</b> |       |       |       |       |       |       |       |       |       |
| 1990                     | -0.79 | 0.80  | 10.53 | --    | 4.59  | -3.10 | -0.68 | 0.43  | -3.47 |
| 1995                     | -1.02 | 0.40  | 14.27 | --    | 3.01  | 0.89  | 0.30  | 2.29  | 0.52  |
| 1996                     | -0.82 | 0.20  | 12.13 | --    | 4.13  | 0.77  | -0.07 | 1.19  | 0.29  |
| <b>Stock Index</b>       |       |       |       |       |       |       |       |       |       |
| 1990                     | --    | 4350  | 1154  | 3024  | 612   | 505   | 696   | 417   | 651   |
| 1995                     | --    | 6933  | 2216  | 13451 | 831   | 1237  | 651   | 637   | 3170  |
| 1996                     | --    | 8187  | 1529  | 10722 | 372   | 594   | 376   | 401   | 1869  |
| <b>Exchange Rate</b>     |       |       |       |       |       |       |       |       |       |
| 1990                     | 4.78  | 31.28 | 1.81  | 7.79  | 25.59 | 2.70  | 707.8 | 1843  | 24.31 |
| 1995                     | 8.35  | 27.78 | 1.42  | 7.74  | 24.92 | 2.50  | 771.3 | 2249  | 25.71 |
| 1996                     | 8.31  | 27.37 | 1.41  | 7.73  | 25.34 | 2.52  | 804.5 | 2342  | 26.22 |
| <b>FRs in Mo of Imp.</b> |       |       |       |       |       |       |       |       |       |
| 1990                     | --    | 10.3  | 6.9   | 3.1   | 4.5   | 3.7   | 2.3   | 3.2   | 0.8   |
| 1995                     | --    | 11.2  | 6.2   | 3.1   | 5.4   | 3.1   | 2.5   | 2.9   | 2.3   |
| 1996                     | --    | 10.5  | 7.6   | 3.5   | 5.4   | 3.7   | 2.3   | 3.6   | 2.8   |

|   | CHI | TWN | SNG | HKG | THD  | MAL | KOA | IND  | PHN  |
|---|-----|-----|-----|-----|------|-----|-----|------|------|
| <b>Bank Lending Boom Measure (%)</b>                | 9   | 14  | 16  | 14  | 51   | 27  | 17  | 12   | 152  |
| <b>Non-performing Loan Percentage (%)</b>           | 14  | 4   | 4   | 4   | 19   | 16  | 16  | 17   | 14   |
| <b>Foreign Debt to GDP Ratio</b>                    | 1/6 | <1% | <1% | <1% | 1/3  | 2/5 | 1/7 | >1/2 | >3/5 |
| <b>Short-term Debt to Total Debt Ratio (%)</b>      | 15  | <10 | <10 | <10 | 30   | 20  | 25  | 15   | 15   |
| <b>Short-term Debt to Foreign Reserve Ratio (%)</b> | 30  | <10 | <10 | <10 | >50  | 25  | >50 | >120 | >80  |
| <b>Liability to Asset Ratio</b>                     | 1.2 | 0.6 | 1.6 | 1.7 | 10.8 | 1.5 | 3.6 | 4.2  | 1.7  |



- Possible Explanation of 1997 Asian Crisis: The possibility of discrete equilibrium shifts may be the only explanation for sudden, large scale and wide spread financial crisis in high performing East Asian countries.
- Hwang-Jiang-Wang (2004): with interplays by financial intermediaries, large businesses (chaebols) and politicians,
  - there are endogenous financial institutions and incentive mechanisms adjusting in response to economic primitives
  - leading to multiple equilibria, one with collusion (no effort devoted to clean institutions) and another with no collusion

- Collusion vs. no-collusion equilibrium

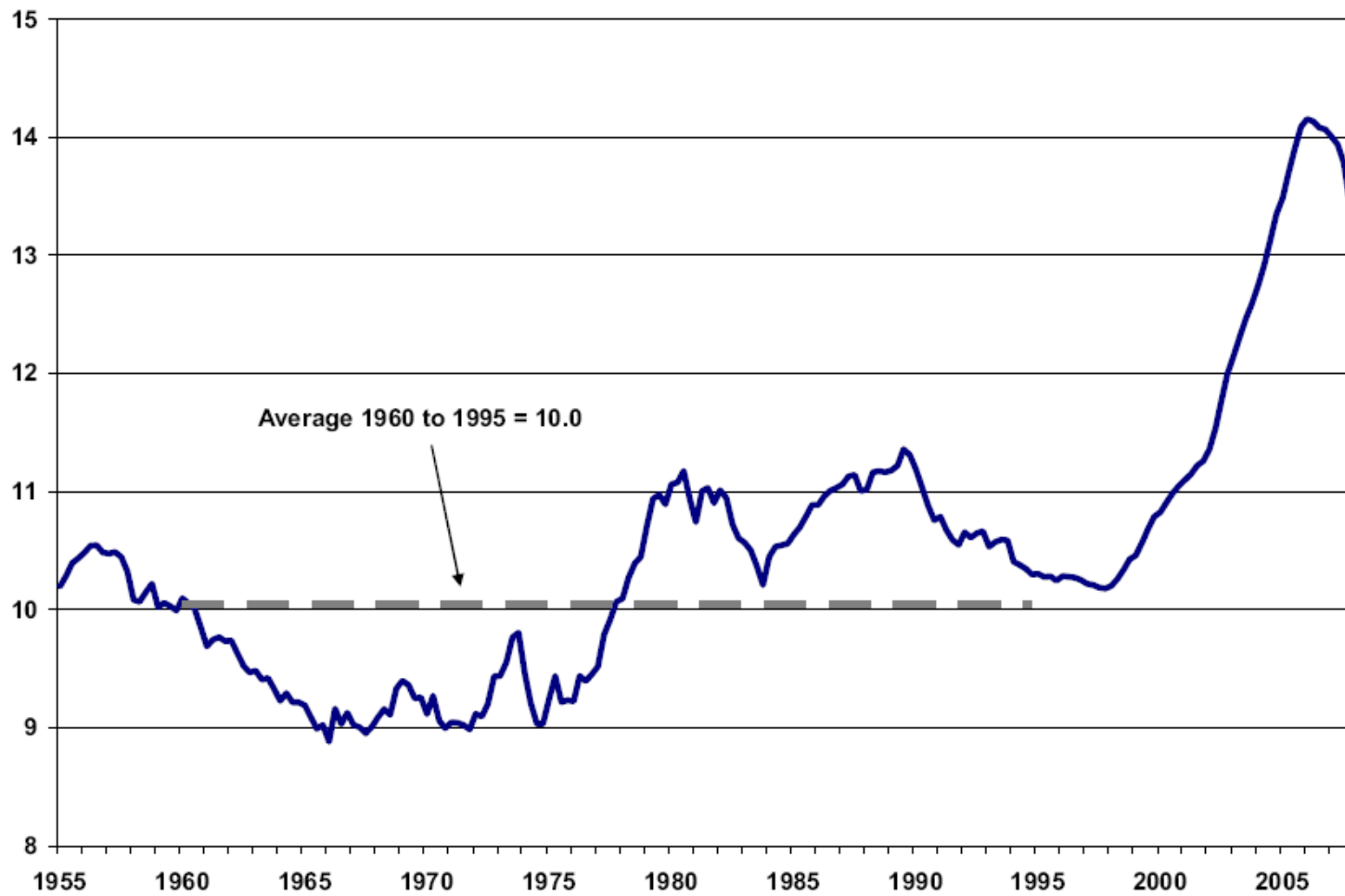


- FI's iso-profit curves (upward-sloping) may intersect at  $N(v)$  with political token  $> 0$  or at  $C(v)$  with token  $= 0$

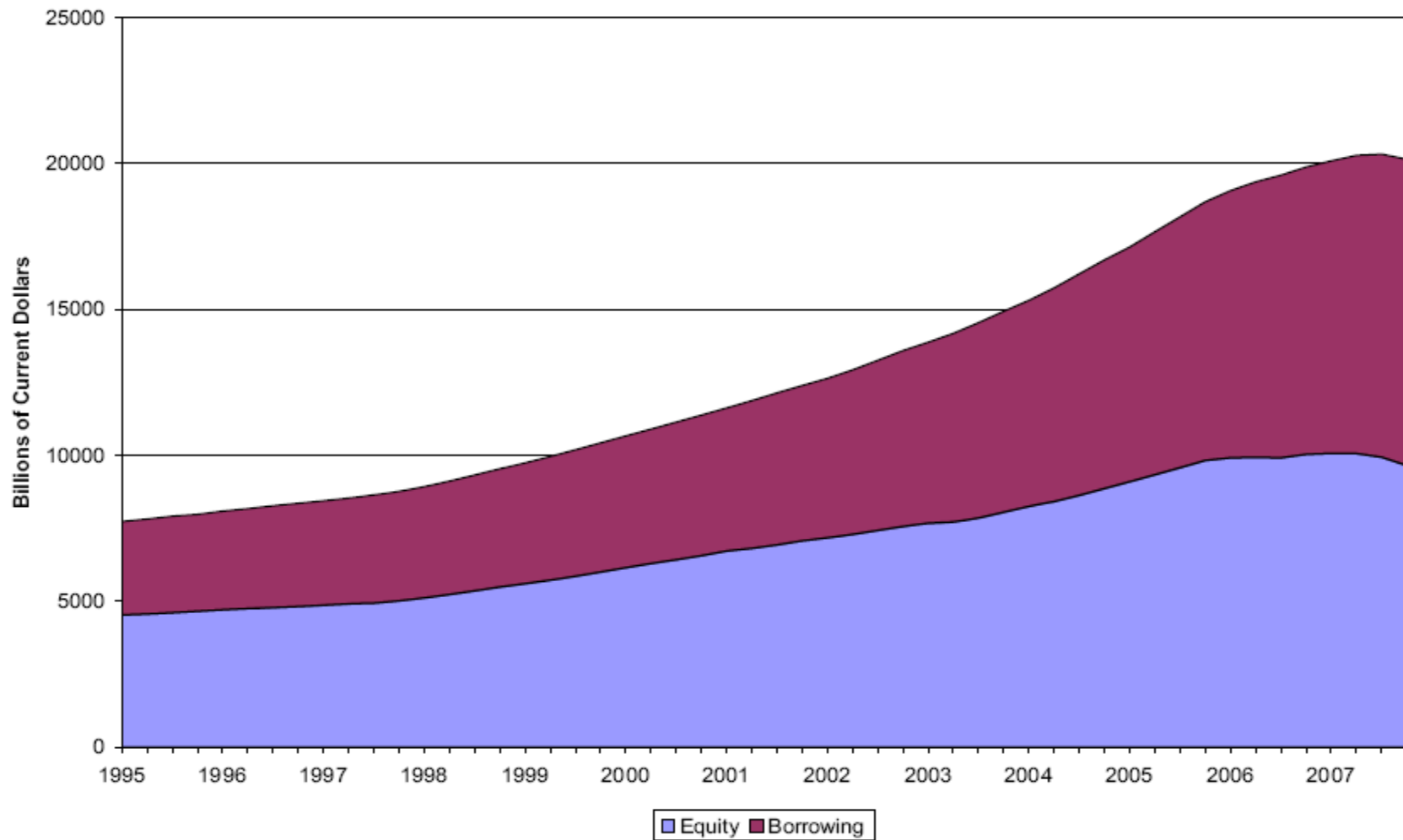
## e. The Financial Tsunami

- Two Primary Causes:
  - Financial deregulation since 1992, resulting in severe moral hazard problems
    - subprime lending by government sponsored Fannie Mae/Freddie Mac
    - wide acceptance of risky insuees with low prenum by AIG
  - Widely linked financial derivatives, causing wide spread of crises (putting all bad eggs in one basket, facing many financial firms, such as Bear Stearns & Lehman Brothers)

- Home Price-Rent Ratio

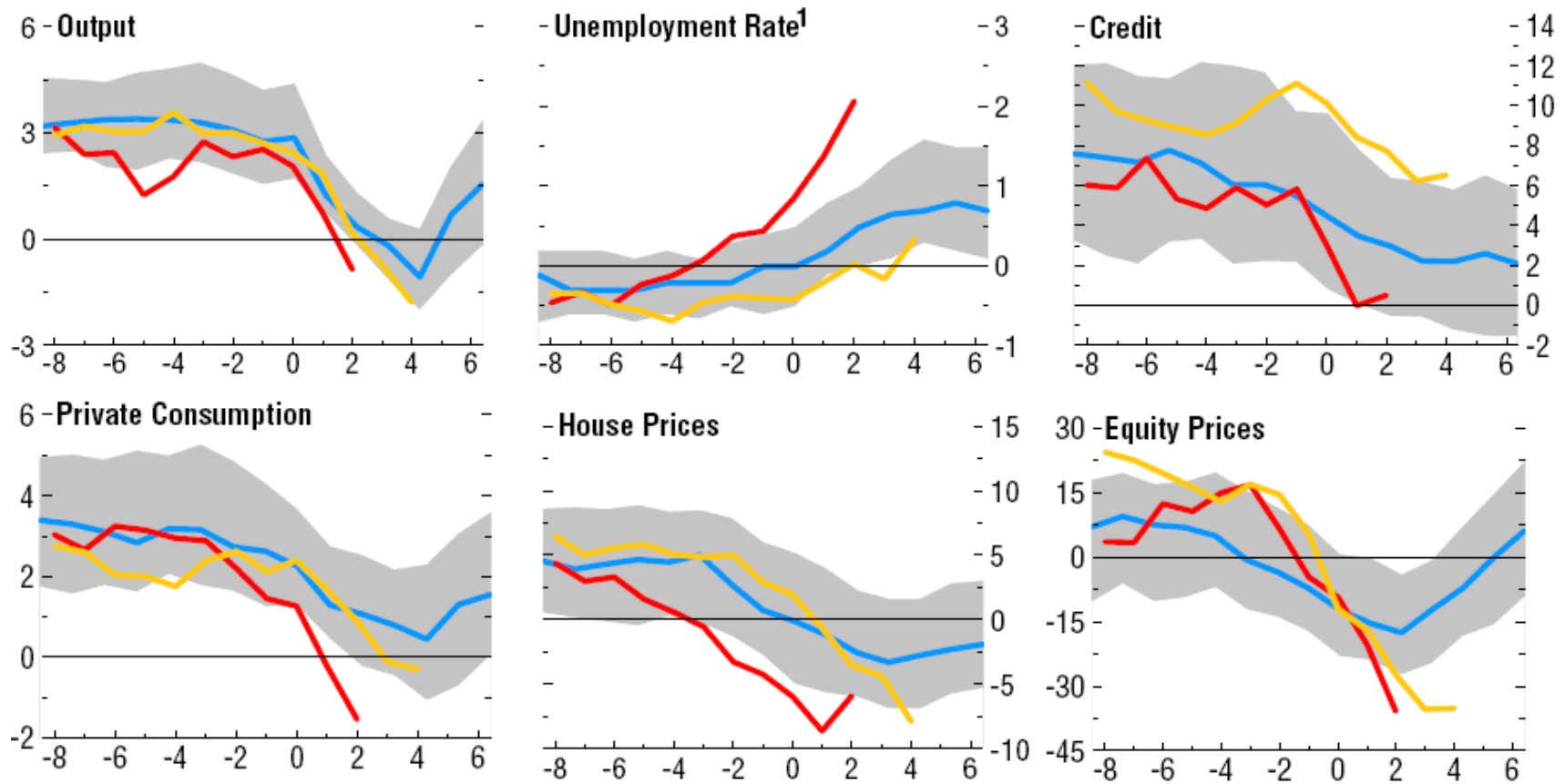


- Housing Equity vs. Borrowing

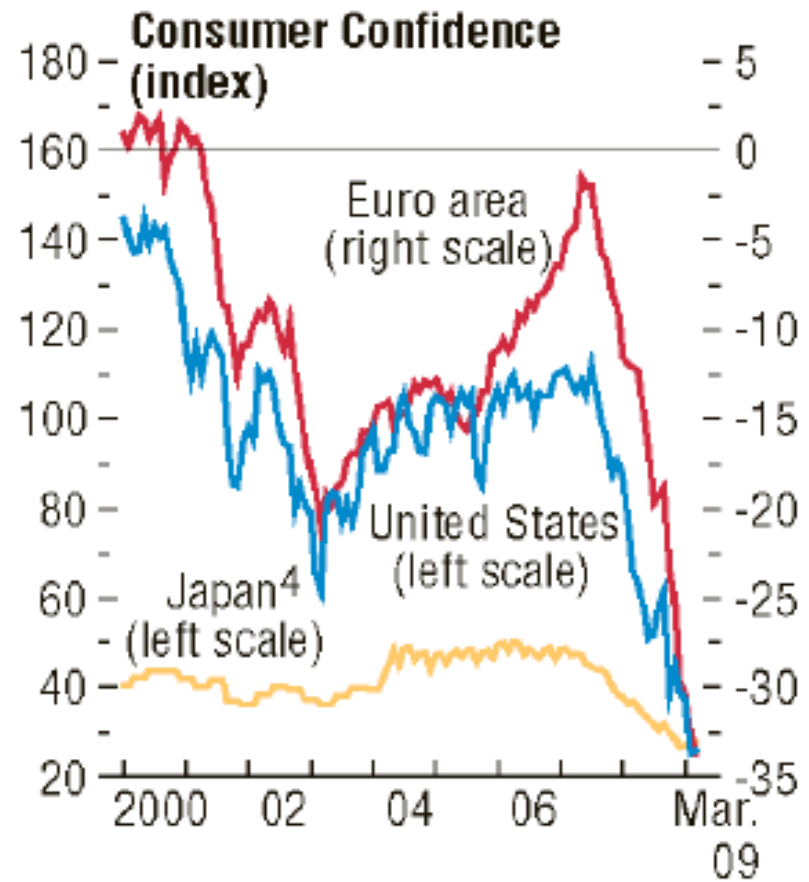
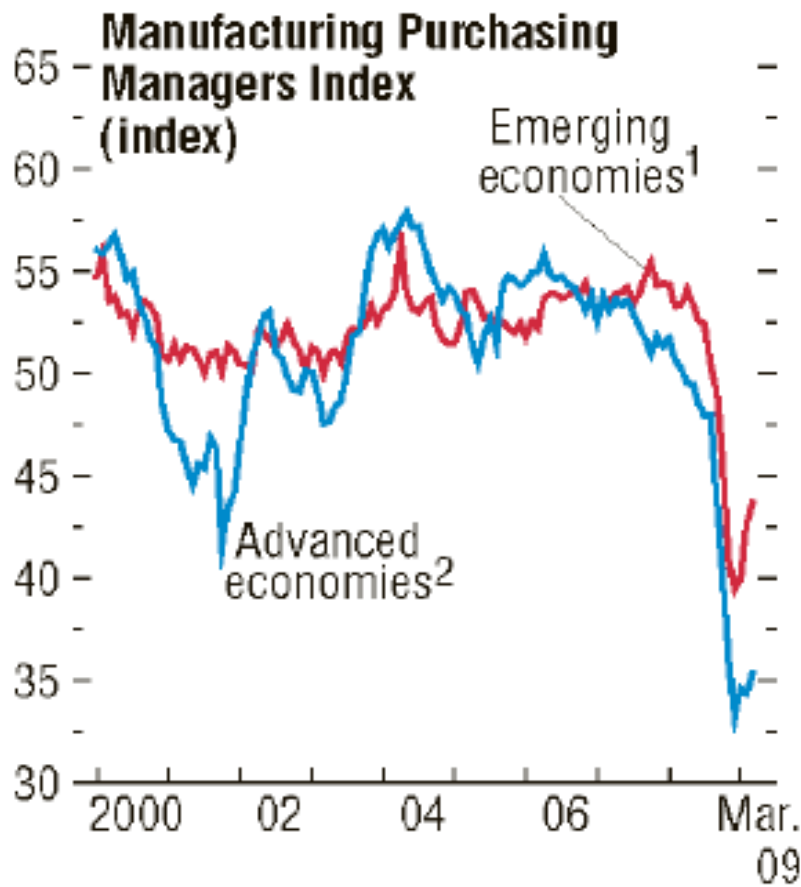


- Severity of Recessions Compared

Current U.S. vs. Current Others & Previous U.S.



- Managers and Consumers Indexes



- Big Push or Big Crash

- The Financial Tsunami can be explained by interplays between financial institutions and market participations
- Becsi-Wang-Wynne (1999): There are market participation externalities
  - Production efficiency (PE) describes a positive relationship between market thickness and market returns
  - Bank break-even (BB) can be normal, downward-sloped (thicker markets require lower loan rates to break even), but can also be upward-sloping when there are strong market participation externalities (higher loan rates => higher expected return => thicker markets)
  - With upward-sloping BB, there can be co-existence of a good equilibrium (big push) and a bad equilibrium (big crash)



# Bank Breakeven (BB) vs. Production Efficiency (PE)

