

# MOST 2014 學術研習營 (貨幣政策與匯率動態)

貨幣政策與匯率動態

陳旭昇

國立台灣大學經濟系

2014.11.10

# Outline

- 1 Measuring Monetary Policy
- 2 A Quick Review of VAR Models
- 3 Structural Vector Autoregressions
- 4 Identification
- 5 Monetary Policy and VAR
- 6 Monetary Policy and Exchange Rate Dynamics

# Measuring Monetary Policy

## (1) Conventional Naive Measure:

- ▶ Money Supply (Friedman and Schwartz)
  - ★ In Friedman and Schwartz (1963) there are a few examples where changes in the money supply are clearly exogenous (i.e., they are not caused by changes in output).
  - ★ Example: The increase in reserve requirements in 1936-7 so that the Federal Reserve could improve its control of the money supply. This reduced the rate of money growth and led to a severe recession in 1937-8.
- ▶ Short-run Interest Rate

Problem: mixture of exogenous and endogenous shocks

# Measuring Monetary Policy

## (2) Narrative Approach (Romer and Romer dates)

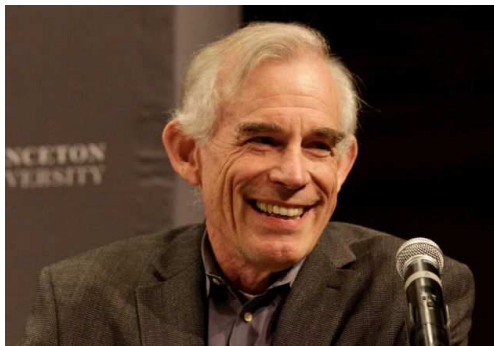
- ▶ Romer and Romer (1989, NBER Macro) Romer and Romer (1994, JME), Romer and Romer (2004, AER)
- ▶ Based on Federal Reserve documents, six times are identified that the Fed appeared to shift to tighter monetary policy not in response to real activities.
- ▶ Problem: **indeed exogenous?**
- ▶ See the critiques by Leeper (1997, JME)

# Measuring Monetary Policy

## (3) VAR Approach

- ▶ Exogenous/unanticipated shocks
- ▶ VAR Models are now used as a central tool in empirical macroeconomics.
- ▶ Sims (1980, *Econometrica*) provided a new macro-econometric framework that held great promise.
  - ★ Christiano (2012) “ Christopher A. Sims and Vector Autoregressions ”  
*Scandinavian Journal of Economics*

# Christopher Sims



- Christopher A. Sims (1942–), Princeton University. Nobel Laureate (2011)

# VAR Models

Types of VAR:

- 1 Reduced-form VAR (simply, VAR)
- 2 Structural VAR (SVAR)
  - ▶ Recursive VAR, Semi-structural VAR
  - ▶ Non-recursive VAR, Structural VAR

# Structural VAR

- Given  $y_t \in \mathbb{R}^k$ , the SVAR( $p$ ) model is

$$y_t = D_0 y_t + D_1 y_{t-1} + \cdots + D_p y_{t-p} + B e_t$$

$$e_t \sim^{i.i.d.} (0, I) \quad \text{structural shock}$$

- (a) Note that there exist contemporary effects ( $D_0$  matrix)
- (b)  $[D_0]_{jj} = 0$ ,  $j = 1, \dots, k$  (standardization)
- (c)  $B$  diagonal matrix (orthogonalization condition)
- (d) The restrictions on  $D_0$  depend on economic theory



# Structural VAR

- Given SVAR,

$$y_t = D_0 y_t + D_1 y_{t-1} + \cdots + D_p y_{t-p} + B e_t, \quad e_t \sim^{i.i.d.} (0, I)$$

- With a few more manipulations, we obtain a reduced-form VAR

$$y_t = \Phi_1 y_{t-1} + \cdots + \Phi_p y_{t-p} + \varepsilon_t$$

where  $\Phi_j \equiv (I - D_0)^{-1} D_j$  and  $\varepsilon_t \equiv (I - D_0)^{-1} B e_t$

# Identification

- SVAR vs. VAR

$$y_t = D_0 y_t + D_1 y_{t-1} + \cdots + D_p y_{t-p} + B e_t$$

$$y_t = \Phi_1 y_{t-1} + \cdots + \Phi_p y_{t-p} + \varepsilon_t$$

- ▶ Our goal is to **identify**  $\{D_0, D_1, \dots, D_p\}$  and  $B$  from  $\{\Phi_1, \Phi_2, \dots, \Phi_p\}$  and  $\Sigma_\varepsilon$
- ▶ Note that

$$D_j = (I - D_0)\Phi_j, \quad j = 1, \dots, p$$

the **identification** can be achieved by

$$\varepsilon_t = (I - D_0)^{-1} B e_t$$

# Identification

- From  $\varepsilon_t = (I - D_0)^{-1} B e_t$ ,

$$E(\varepsilon_t \varepsilon_t') = (I - D_0)^{-1} B E(e_t e_t') B' (I - D_0)^{-1'}$$

- That is,

$$\Sigma_\varepsilon = (I - D_0)^{-1} B B' (I - D_0)^{-1'}$$

- ▶  $\frac{k(k-1)}{2} + k$  parameters can be identified from  $\Sigma_\varepsilon$
- ▶ On the other hand, we need to identify  $2k^2$  parameters in  $D_0$  and  $B$
- ▶ Thus, the difference is  $\frac{k(3k-1)}{2}$

# Identification

- Recall that
  - $B$  is diagonal (structural shocks are uncorrelated to each other).
  - Standardization:  $[D_0]_{jj} = 0, j = 1, \dots, k$
- These conditions imply

$$\underbrace{k^2 - k}_{\text{by}(a)} + \underbrace{k}_{\text{by}(b)}$$

We still need to identify

$$\frac{k(3k - 1)}{2} - (k^2 - k) - k = \frac{k(k - 1)}{2}$$

# Identification

- How to obtain  $\frac{k(k-1)}{2}$  conditions?
  - ▶ short-run restriction
    - (a) recursive (semi-structural)
    - (b) economic theory/institutional knowledge (structural)
  - ▶ long-run restriction
- See:
  - ▶ Sims (1980, Econometrica)
  - ▶ Bernanke (1986, Carnegie-Rochester Conference Series on Public Policy)
  - ▶ Blanchard and Quah (1989, AER)

# Monetary Policy and VAR

## Puzzles in Previous Studies

A conventional SVAR:  $(Y, P, M, R)$  with structural shocks  $(e_y, e_p, e_M, e_R)$

- Is the monetary shock  $e_M$  or  $e_R$ ?
- Two puzzles:
  - ▶ Liquidity Puzzle ( $e_M \Rightarrow R$ )

	Theory	Evidence
$M_t^s \uparrow$	$R_t \downarrow$	$R_t \uparrow$

- ▶ Price Puzzle ( $e_R \Rightarrow P$ )

	Theory	Evidence
$R_t \uparrow$	$P_t \downarrow$	$P_t \uparrow$

# Monetary Policy and VAR

More Sophisticated Structure: Reserve Market.

- Bernanke and Blinder (1992, AER): Federal Funds Rates
- Christiano and Eichenbaum (1992): Non-borrowed Reserves
- Strongin (1995, JME): Non-borrowed Reserves/Total Reserves
- Cosimano and Sheehan (1994, JMacro): Borrowed Reserves
- Bernanke and Mihov (1998, QJE) consider all of the above models

# Bernanke and Mihov (1998)

Consider a 6-Variable SVAR

- Macroeconomic Variables
  - ▶ real GDP
  - ▶ GDP deflator
  - ▶ commodity prices
- Policy Variables
  - ▶ total bank reserves
  - ▶ non-borrowed reserves
  - ▶ federal funds rates



# Identification in Bernanke and Mihov (1998)

- Let

$$Y_t = \begin{bmatrix} \text{Real GDP} \\ \text{GDP deflator} \\ \text{Commodity Price} \end{bmatrix}, \quad P_t = \begin{bmatrix} TR_t \\ NBR_t \\ FF_t \end{bmatrix}$$

- Consider a SVAR

$$Y_t = \sum_{i=0}^k B_i Y_{t-i} + \sum_{i=0}^k C_i P_{t-i} + A^y v_t^y$$

$$P_t = \sum_{i=0}^k D_i Y_{t-i} + \sum_{i=0}^k G_i P_{t-i} + A^p v_t^p$$

- Bernanke and Mihov (1998) assume  $C_0 = \mathbf{0}$

# Identification in Bernanke and Mihov (1998)

- We can estimate a reduced form VAR

$$Y_t = \sum_{i=1}^k H_i^y Y_{t-i} + \sum_{i=1}^k H_i^p P_{t-i} + \varepsilon_t^y$$

$$P_t = \sum_{i=0}^k J_i^y Y_{t-i} + \sum_{i=1}^k J_i^p P_{t-i} + \varepsilon_t^p$$

where

$$\varepsilon_t^p = (I - G_0)^{-1} A^p v_p \quad \text{or} \quad (I - G_0) \begin{bmatrix} \varepsilon_t^{TR} \\ \varepsilon_t^{NBR} \\ \varepsilon_t^{FF} \end{bmatrix} = A^p \begin{bmatrix} v_t^d \\ v_t^b \\ v_t^s \end{bmatrix}$$

# Identification in Bernanke and Mihov (1998)

- Open-market operations to affect reserve market
- Reserve Market

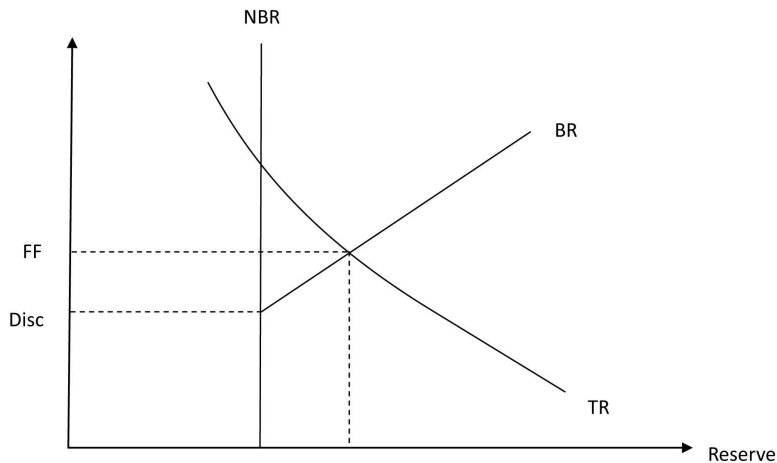
$$\varepsilon_t^{TR} = -\alpha\varepsilon_t^{FF} + v_t^d, \quad (1)$$

$$\varepsilon_t^{BR} = \beta(\varepsilon_t^{FF} - \varepsilon_t^{DISC}) + v_t^b, \quad (2)$$

$$\varepsilon_t^{NBR} = \phi^d v_t^d + \phi^b v_t^b + v_t^s. \quad (3)$$

$$\varepsilon_t^{TR} = \varepsilon_t^{BR} + \varepsilon_t^{NBR} \quad (4)$$

# Reserve Market



# Identification in Bernanke and Mihov (1998)

- Assume  $\varepsilon_t^{DISC} = 0$ ,

$$\underbrace{\begin{bmatrix} 1 & 0 & \alpha \\ 1 & -1 & -\beta \\ 0 & 1 & 0 \end{bmatrix}}_{I-G_0} \begin{bmatrix} \varepsilon_t^{TR} \\ \varepsilon_t^{NBR} \\ \varepsilon_t^{FF} \end{bmatrix} = \underbrace{\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ \phi^d & \phi^b & 1 \end{bmatrix}}_{A^p} \begin{bmatrix} v_t^d \\ v_t^b \\ v_t^s \end{bmatrix}$$

# Measuring Monetary Policy

We can thus solve for  $v_t^s$  as

$$v_t^s = -(\phi^d + \phi^b)\varepsilon_t^{TR} + (1 + \phi^b)\varepsilon_t^{NBR} - (\alpha\phi^d - \beta\phi^b)\varepsilon_t^{FF}.$$

# Measuring Monetary Policy

1. FFR Model:  $\phi^d = 1, \phi^b = -1,$

$$v_t^s = -(\alpha + \beta)\varepsilon_t^{FF}.$$

2. NBR Model:  $\phi^d = 0, \phi^b = 0,$

$$v_t^s = \varepsilon_t^{NBR}.$$

3. NBR/TR Model:  $\alpha = 0, \phi^b = 0,$

$$v_t^s = -\phi^d \varepsilon_t^{TR} + \varepsilon_t^{NBR}.$$

4. BR Model:  $\phi^d = 1, \phi^b = \alpha/\beta,$

$$v_t^s = -\left(1 + \frac{\alpha}{\beta}\right) (\varepsilon_t^{TR} - \varepsilon_t^{NBR}).$$

5. JI Model:  $\alpha = 0,$

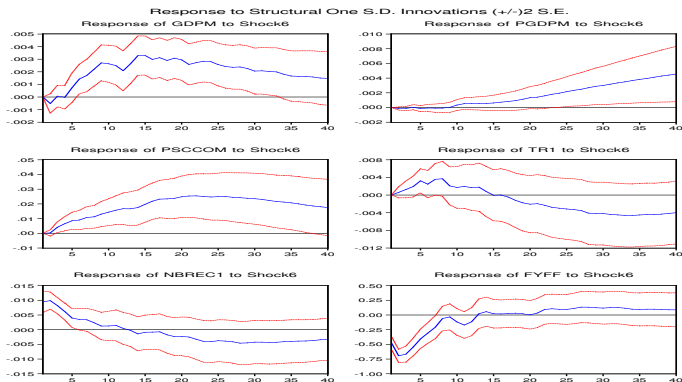
$$v_t^s = -(\phi^d + \phi^b)\varepsilon_t^{TR} + (1 + \phi^b)\varepsilon_t^{NBR} + \beta\phi^b\varepsilon_t^{FF}.$$

# Identification: An Alternative Representation

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ d_{21} & 1 & 0 & 0 & 0 & 0 \\ d_{31} & d_{32} & 1 & 0 & 0 & 0 \\ d_{41} & d_{42} & d_{43} & 1 & 0 & \alpha \\ d_{51} & d_{52} & d_{53} & 1 & -1 & -\beta \\ d_{61} & d_{62} & d_{63} & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \varepsilon_t^{GDP} \\ \varepsilon_t^P \\ \varepsilon_t^{Pcm} \\ \tilde{\varepsilon}_t^{TR} \\ \tilde{\varepsilon}_t^{NBR} \\ \tilde{\varepsilon}_t^{FF} \end{bmatrix} \\
 = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \phi^d & \phi^b & 1 \end{bmatrix} \begin{bmatrix} v_{1t}^{NP} \\ v_{2t}^{NP} \\ v_{3t}^{NP} \\ v_t^d \\ v_t^b \\ v_t^s \end{bmatrix}$$



# Impulse Responses: Expansive Monetary Shock



- Hump-shaped and Significant Response of Real Output
- Liquidity Effect
- No Price Puzzle

## Summary: VAR Models as Measures of Monetary Policy

- Incorporate the effects of possible changes in reserve-market structure and in the Fed's operating procedures.
- Can be generalized to other countries or periods.
- For instance,  
公開市場操作為中央銀行經由金融市場，買賣票債券的方式增減銀行體系的準備金，以調控準備貨幣與拆款市場利率的操作機制，為中央銀行最重要的貨幣政策工具。(中華民國中央銀行之制度與功能, 2003)

# Recent Developments

- Alternative Identification Schemes:
  - ▶ Sign Restrictions: Uhlig (2005, JME)
  - ▶ Identification through Heteroskedasticity: Rigobon (2003, REStat), Rigobon and Sack (2003, QJE) and Rigobon and Sack (2004, JME), Lanne and Lutkepohl (2008, JMCB)
- Factor-augmented VAR
  - ▶ Bernanke et al. (2005, QJE)

## Sign Restrictions

- Uhlig (2005, JME)
- Method: impose all the other sign restrictions, but not the restriction on output and total reserves.

Series	Response restricted?
Real output	no
GDP deflator	Negative or zero
Commodity price index	Negative or zero
Total Reserves	no
Nonborrowed Reserves	Negative or zero
Federal Funds Rate	Positive or zero

The restrictions are for horizons  $k$ ,  $k = 0, \dots, K$ .

## Identification through Heteroskedasticity

- Rigobon (2003, REStat), Rigobon and Sack (2003, QJE) and Rigobon and Sack (2004, JME)
- Example:

$$p_t = \beta q_t + \varepsilon_t$$

$$q_t = \alpha p_t + \eta_t$$

where  $\sigma_{\varepsilon, \eta} = 0$  (structural shocks are orthogonal)

- 4 unknown:  $\alpha$ ,  $\beta$ ,  $\sigma_{\varepsilon}^2$ , and  $\sigma_{\eta}^2$  (not identified)

$$\begin{bmatrix} \text{Var}(p_t) & \text{Cov}(p_t, q_t) \\ \text{Cov}(q_t, p_t) & \text{Var}(q_t) \end{bmatrix} = \frac{1}{(1 - \alpha\beta)^2} \begin{bmatrix} \beta^2 \sigma_{\eta}^2 + \sigma_{\varepsilon}^2 & \beta \sigma_{\eta}^2 + \alpha \sigma_{\varepsilon}^2 \\ \cdot & \sigma_{\eta}^2 + \alpha^2 \sigma_{\varepsilon}^2 \end{bmatrix}$$

# Identification through Heteroskedasticity

- Assume there are two regimes in the variances of the structural shocks: high and low ( $s \in \{1, 2\}$ ).

$$\hat{\Omega}_s = \frac{1}{(1 - \alpha\beta)^2} \begin{bmatrix} \beta^2 \sigma_{\eta,s}^2 + \sigma_{\varepsilon,s}^2 & \beta \sigma_{\eta,s}^2 + \alpha \sigma_{\varepsilon,s}^2 \\ \cdot & \sigma_{\eta,s}^2 + \alpha^2 \sigma_{\varepsilon,s}^2 \end{bmatrix}$$

- 6 unknown:  $\alpha$ ,  $\beta$ ,  $\sigma_{\varepsilon,1}^2$ ,  $\sigma_{\varepsilon,2}^2$ ,  $\sigma_{\eta,1}^2$ , and  $\sigma_{\eta,2}^2$

# Factor Augmented VAR

- Bernanke et al. (2005, QJE)
- The joint dynamics of unobserved factors  $F_t$  and observable economic variables  $Y_t$  are

$$\begin{bmatrix} F_t \\ Y_t \end{bmatrix} = \Phi(L) \begin{bmatrix} F_{t-1} \\ Y_{t-1} \end{bmatrix} + v_t.$$

- Observation equation:

$$X_t = \Lambda_f F_t + \Lambda_y Y_t + u_t,$$

where  $X_t$  are a number of informational time series.

# Monetary Policy and Exchange Rate Dynamics

## Early Work: Recursive VAR

- Eichenbaum and Evans (1995, QJE).

- ▶ Identification (Wold ordering):

$$[Y_t \quad P_t \quad NBRX_t \quad (R_t^{For} - R_t^{US}) \quad S_t^{For}]'$$

- ▶ Findings:
  - (a) Delayed overshooting
  - (b) U.S. contractionary monetary shocks lead to U.S. dollar appreciation
  - (c) Significant and persistent deviations from UIP (forward discount puzzle)
- ▶ Further readings: Faust and Rogers (2003, JME), Faust et al. (2003, JEEA).



# Monetary Policy and Exchange Rate Dynamics

## Further Investigations

- Structural VAR: Kim and Roubini (2000, JME)
- Sign Restrictions: Scholl and Uhlig (2008, JIE)
- Long-run Restriction: Bjornland (2009, JIE)
- Heteroskedasticity: Caporale et al. (2005, JIMF)
- FVAR: Mumtaz and Surico (2009, JMCB).

## References I

- Bernanke, Ben, Boivin, Jean, and Elias, Piotr S. (2005), “Measuring the effects of monetary policy: A factor-augmented vector autoregressive (favar) approach”, *The Quarterly Journal of Economics*, 120(1), 387–422.
- Bernanke, Ben S. (1986), “Alternative explanations of the money-income correlation”, *Carnegie-Rochester Conference Series on Public Policy*, Elsevier, 25(1), 49–99.
- Bernanke, Ben S and Blinder, Alan S (1992), “The Federal Funds Rate and the Channels of Monetary Transmission”, *American Economic Review*, 82(4), 901–21.
- Bernanke, Ben S. and Mihov, Ilian (1998), “Measuring monetary policy”, *Quarterly Journal of Economics*, 113(3), 869–902.

## References II

- Bjornland, Hilde C. (2009), “Monetary policy and exchange rate overshooting: Dornbusch was right after all”, *Journal of International Economics*, 79(1), 64–77.
- Blanchard, Olivier Jean and Quah, Danny (1989), “The Dynamic Effects of Aggregate Demand and Supply Disturbances”, *American Economic Review*, 79(4), 655–73.
- Caporale, Guglielmo Maria, Cipollini, Andrea, and Demetriades, Panicos O. (2005), “Monetary policy and the exchange rate during the asian crisis: identification through heteroscedasticity”, *Journal of International Money and Finance*, 24(1), 39 – 53.

## References III

- Christiano, Lawrence J. and Eichenbaum, Martin (1992), "Identification and the liquidity effect of a monetary policy shock", in A. Cukierman, Z. Hercowitz, and L. Leiderman (eds.), *Political Economy, Growth, and Business Cycles*, Cambridge MA, MIT Press.
- Cosimano, Thomas F. and Sheehan, Richard G. (1994), "The federal reserve operating procedure, 1984–1990: An empirical analysis", *Journal of Macroeconomics*, 16(4), 573–588.
- Eichenbaum, Martin and Evans, Charles L (1995), "Some Empirical Evidence on the Effects of Shocks to Monetary Policy on Exchange Rates", *The Quarterly Journal of Economics*, 110(4), 975–1009.
- Faust, Jon and Rogers, John H. (2003), "Monetary policy's role in exchange rate behavior", *Journal of Monetary Economics*, 50(7), 1403–1424.

## References IV

- Faust, Jon, Rogers, John H., Swanson, Eric, and Wright, Jonathan H. (2003), "Identifying the Effects of Monetary Policy Shocks on Exchange Rates Using High Frequency Data", *Journal of the European Economic Association*, 1(5), 1031–1057.
- Friedman, Milton and Schwartz, Anna Jacobson (1963), *A Monetary History of the United States, 1867-1960*.
- Kim, Soyoung and Roubini, Nouriel (2000), "Exchange rate anomalies in the industrial countries: A solution with a structural VAR approach", *Journal of Monetary Economics*, 45(3), 561–586.
- Lanne, Markku and Lutkepohl, Helmut (2008), "Identifying monetary policy shocks via changes in volatility", *Journal of Money, Credit and Banking*, 40(6), 1131–1149.

## References V

- Leeper, Eric M. (1997), “Narrative and VAR approaches to monetary policy: Common identification problems”, *Journal of Monetary Economics*, 40(3), 641–657.
- Mumtaz, Haroon and Surico, Paolo (2009), “The Transmission of International Shocks: A Factor-Augmented VAR Approach”, *Journal of Money, Credit and Banking*, Blackwell Publishing, 41(s1), 71–100.
- Rigobon, Roberto (2003), “Identification Through Heteroskedasticity”, *The Review of Economics and Statistics*, 85(4), 777–792.
- Rigobon, Roberto and Sack, Brian (2003), “Measuring The Reaction Of Monetary Policy To The Stock Market”, *The Quarterly Journal of Economics*, 118(2), 639–669.

## References VI

- (2004), “The impact of monetary policy on asset prices”, *Journal of Monetary Economics*, 51(8), 1553–1575.
- Romer, Christina D. and Romer, David H. (1989), “Does Monetary Policy Matter? A New Test in the Spirit of Friedman and Schwartz”, in *NBER Macroeconomics Annual 1989, Volume 4*, NBER Chapters, 121–184, National Bureau of Economic Research, Inc.
- (1994), “Monetary policy matters”, *Journal of Monetary Economics*, 34(1), 75–88.
- (2004), “A New Measure of Monetary Shocks: Derivation and Implications”, *American Economic Review*, 94(4), 1055–1084.

## References VII

- Scholl, Almuth and Uhlig, Harald (2008), “New evidence on the puzzles: Results from agnostic identification on monetary policy and exchange rates”, *Journal of International Economics*, 76(1), 1–13.
- Sims, Christopher A (1980), “Macroeconomics and Reality”, *Econometrica, Econometric Society*, 48(1), 1–48.
- Strongin, Steven (1995), “The identification of monetary policy disturbances explaining the liquidity puzzle”, *Journal of Monetary Economics*, 35(3), 463–497.
- Uhlig, Harald (2005), “What are the effects of monetary policy on output? Results from an agnostic identification procedure”, *Journal of Monetary Economics*, 52(2), 381–419.